# Solubility Study in Ag-Cu Binary System Prepared By Ball Milling Process

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## Abstract:

Solid solutions of Ag-Cu were prepared via ball milling process, for about 5-30 h. The Cu-20at%Ag and Cu-3.64at%Ag composition were investigated by X-ray diffraction technique. It was realized that the solid solubility level could be increased by increasing the initial solute content in the mixture. In addition, shifts in peak positions of silver and copper were observed with milling time. The dissolution volume was estimated by thermodynamic relations and was compared with the measured values using X-ray diffraction technique and it was observed that the measured and calculated volumes agreed well. The final dissolution volume of 39.155 litters was calculated by thermodynamic relationship.

Keywords: copper, silver, solid solution, mechanical alloying.

## **1. INTRODUCTION**

Mechanical alloying process has become a widely used technique to form powder materials and to synthesize a large range of none-equilibrium phases, from amorphous materials to nanocrystalline phases, to extended solid solutions [1-3]. Solid solubility extensions have been achieved in many alloy systems by non-equilibrium processing methods such as RSP and vapor deposition. Similarly, mechanically alloyed powders also exhibit extension of equilibrium solid solubility limits. In addition to synthesizing stable (equilibrium) solid solutions, it has also been possible to synthesize metastable (non-equilibrium) supersaturated solid solutions by mechanical alloying starting from blended elemental powders in several binary and higher order systems [4-10]. Metastable alloys are of great interest due to their novel structure, properties, and applications compared to their equilibrium counter parts. In the present study, the effect of combination on solid solution formation in

Ag-Cu system via mechanical alloying process was investigated.

#### **2- EXPERIMENTAL PROCEDURE**

Cu (MERCK Art No.102703) and Ag (ALDRICH Art No.32707-7) powders were used as starting materials. The powder mixture of Cu-20at%Ag and Cu-3.64at%Ag and hardened steel balls were placed in stainless steel vials hermetically sealed and milled in a planetary ball mill. The weight ratio of the powders to the balls (BPR) was kept at 1:15 for all experiments. Handling of powders and milling process were performed under protection of pure argon gas atmosphere. The vials were rotated at 300 rpm. The mechanically alloyed powders were characterized by X-ray diffraction method using  $CuK\alpha$  radiation. Average grain sizes of Cu and Ag phases were estimated by the peak broadening of the X-ray diffraction patterns by using Wiliamson Hall method base on the formula (1) [12].



*Figure 1: X-ray diffraction pattern of (a): as received Ag and Cu powders (b): Cu-20 at.%Ag (c): Cu-3.64at.% Ag at different milling times 5, 15 and 30 h* 



Figure 2: The average grain size of Ag vs. milling time

$$b\cos\theta = \frac{0.9\lambda}{d} + 2\eta\sin\theta \tag{1}$$

Where  $\eta$  is strain in lattice,  $\lambda$  is wave length,  $\theta$  is Bragg angle, b is full-width at halfmaximum (FWHM) of the Bragg peaks and d is grain size.

# **3- RESULT AND DISCUSSION**

Increasing the milling time of pure silver and copper powders gave rise to the broadening of the X-ray diffraction peaks and reducing the intensity of certain peak such as the one at (111). These were due to the formation of nanometer-size coherent

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diffraction domains and the accumulation of lattice defects. However, the peak positions of silver and copper hardly changed with milling time. When aforementioned mechanical mixtures were milled, local mutual dissolution processes formed a new face-centered cubic (fcc) phase with its (111) peak positioned between the (111) reflections of Ag and Cu, as shown in Figure 1. A shift in the diffraction peaks of Cu towards lower angles was the result of an increase in lattice constant which consequently referred to the dissolution of Ag into Cu. In contrast a shift in the diffraction peak of Ag towards upper angles suggested a decrease in lattice constant due to dissolution of Cu into Ag owing to smaller atomic radius of Cu. It is worth noting that the atomic radii of Cu and Ag are 0.128 nm and 0.144 nm, respectively. The average grain sizes of Ag phase in both mixtures were estimated by the peak broadening of X-ray diffraction peaks and the Williamson Hall method as shown in Figure 2.



Figure 3: Lattice parameter changes of Cu vs. milling times

Figure 3 depicts the changes in the lattice parameter of Cu as a function of milling time for both mixtures.



*Figure 4:* Dissolution volume percent accompanying the formation of Cu-20%atAg solid solution

## **4-THERMODYNAMICAL INVESTIGATION**

Gibbs free energy of a solution may be written as follow [11]:

$$\Delta G^M = RT(X_A \ln a_A + X_B \ln a_B) \qquad (eq.1)$$

Where  $\Delta G^M$  is the change in the molar Gibbs free energy by the solution,  $x_A$  and  $x_B$  are the mole fraction of A and B in the solution, R and T are universal gas constant and temperature, respectively and the *a* denotes activity. Also:

$$a_A = X_A \cdot \gamma_A \tag{eq.2}$$

Where  $\gamma$  is the activity coefficient. For the component i:

$$\Delta \overline{G_i^M} = RT \ln a_i \tag{eq.3}$$

The quantity is designated as  $\Delta G_i^M$ , the partial molar Gibbs free energy of the solution of i. The general thermodynamic relationship for the state properties of a system is applicable to the partial molar properties of components of a system. Thus, for the component i present in a solution:

$$\left(\frac{\partial \overline{G_i}}{\partial P}\right)_{T,Comp} = \overline{V_i} \tag{eq.4}$$

And for the pure component i:

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$$\left(\frac{\partial G^{0}_{i}}{\partial P}\right)_{T,Comp} = V_{i}^{0}$$
(eq.5)

The partial molar volume change accompanying the formation of a solution  $(\Delta V_i^M)$  is defined as:

$$\left[\frac{\partial \Delta \overline{G_i^M}}{\partial P}\right]_{T,comp} = \Delta \overline{V_i^M}$$
(eq.6)

When  $x_i$  is not a function of pressure, then:

$$\left[\frac{\partial \ln \gamma_i}{\partial p}\right]_{T,comp} = \frac{\Delta V_i^M}{RT}$$
(eq.7)



Figure 5: Scanning electron microscopy (SEM) and Cu dot maps of Cu-20 at.%Ag powder milled for 5 h a) BS and b) SE 15h c) BS and d) SE 30h e) BS and f) SE

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In the present study, the dissolution volume calculated from the thermodynamic relations was in a good agreement with the one measured using the X-ray diffraction. In this way, shift peak shows change of lattice parameter and volume due to diffusion. In the other hand, the final dissolution volume was calculated using equation 7. For calculating the temperature value, equation 8 was used. The final dissolution volume was measured to be 39.155 litters using equation 7. A complete dissolution was achieved after 30h of milling, as shown in Figure 4.

$$T' = T(1 + \frac{D_{bal}}{D_{chim}})$$
(eq.8)

(T' = 573K, P=1.2atm), T' is effective temperature for alloying, which is equivalent to a rise in the temperature of the system to (> T= ambient temperature). Furthermore, it was proposed that T'is related to T through the following relationship. Where,  $D_{bal}$  and  $D_{chim}$  are the ballistic and chemical inter diffusion coefficients, respectively. It may be pointed out that  $D_{chim}$  is exponentially related with temperature, while  $D_{bal}$  is considered to be temperature independent [13].

Figure 5 shows SEM images and the Cu dot maps of Cu-20 at. %Ag powder after milling for different durations.

### **5- CONCLUSIONS**

Mechanical alloying process was performed in the Ag-Cu system. It was shown that the solid solubility level rose by increasing the initial solute content in a powder mixture. The shifts in the position of peaks in the X-ray diffraction patterns were utilized to determined changes in the lattice parameter values and calculated the solid solubility levels. The final dissolution volume calculated by thermodynamic relationships was 39.155 litters. This calculated volume was in a good agreement with the one measured by the X-ray diffraction method. The results suggested that XRD patterns could be a reliable method in quantifying the phase transformation thermodynamics of solid phases subjected to mechanical alloying.

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