Design and Test of New Robust QCA Sequential Circuits

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Abstract

One of the several promising new technologies for computing at nano-scale is quantum-dot cellular automata (QCA). In this paper, new designs for different QCA sequential circuits are presented. Using an efficient QCA D flip-flop (DFF) architecture, a 5-bit counter, a novel single edge generator (SEG) and a divide-by-2 counter are implemented. Also, some types of oscillators, a new edge-triggered Kpulse generator (KPG) and a negative pulse generator (NPG) are presented for implementation in QCA. The robust layouts of proposed circuits are designed, implemented and simulated using QCADesigner software without any wire crossing. The fault effects at the output of proposed DFF due to the missing cell defects are analyzed. Also, the robustness of the proposed QCA designs with respect to temperature variations is examined. The proposed designs are compared with the previous QCA works and conventional CMOS technology. The simulation results confirm that the novel QCA architectures work properly and can be simply used in designing of QCA sequential circuits.

Keywords: Quantum-dot cellular Automata, QCADesigner, Sequential Circuits, Simulation.

1. INRODUCTION

Research into nanoscale electronics has increased significantly over the last decade. VLSI technology is going to approach a scaling limit in deep nanometer regime. International Technology Roadmap for Semiconductors (ITRS) [1] reports several possible technology solutions to replace the current CMOS technology. Quantum-dot cellular automata (QCA) may overcome some of the limitations of current technologies, because it not only gives a solution at the nanoscale, but also it offers new methods of computation and information transformation [2-6]. In conventional logic circuits information is transferred by electrical current, but QCA operates using the Columbic interaction that connects the state of one QCA cell to the state of its neighbors. High density, fast speed, switching and low power dissipation are the advantages of QCA circuits over the current CMOS technology. QCA sequential circuits

design has not been fully addressed in the previous literature. In [7], D flip-flop, Gated D flip-flop, T flip-flop, SR active high flip-flop, SR active low flip-flop, JK flip-flop, 2-bit counter and 4-bit shift register were designed and simulated. Several designs of QCA sequential circuits such as Gated D latch, RS latch, JK flipflop, T flip-flop, D flip-flop, 2-bit counter, 4-bit counter, and 4-bit shift register were presented in [8]. In [9], novel serial decimal adder and adder/subtractor designs run-time were presented using a reconfigurable wiring approach, which results in further significant OCA hardware simplification. In [10], an optimized QCA LFSR was designed, and then different random number generators (RNGs) using XOR and adder were introduced, which generate different random numbers in each simulation. In [11], a low complexity and energy efficient QCA T flip-flop and high-performance

single-layer synchronous counters were proposed. Also, by cascading the proposed T flip-flop and a suitable level converter a QCA-compatible structure for falling edge triggered T flip-flop was achieved. In [12], using a robust 2:1 multiplexer efficient level triggered and edge triggered QCA flip-flops and memory cell with set/reset ability were introduced. In [13], a robust and efficient QCA design of synchronous counters was proposed. For this means, an innovative design of level-sensitive DFF and appropriate "edge-to-level" an converter were introduced by utilizing of capabilities **OCA** inherent implementations. In [14], two wellorganized JK flip-flop designs and synchronous counters with different sizes were presented.

In this paper, novel designs for different QCA sequential circuits are presented. These designs are introduced for the first time.

The fundamental unit of OCA is the QCA cell [15,16]. A QCA cell (shown in Figure 1a) can be viewed as a set of four charge containers quantum-dots, or positioned at the corners of a square and two extra mobile electrons (free electrons), which can quantum mechanically tunnel between the dots, but not cells. Due to the electrostatic repulsion, the two free electrons only can occupy the corners of the QCA cell, resulting in two specific polarizations as shown in Figure 1a. By using cell polarization P=+1 to represent logic "1" and P=-1 to represent logic "0", binary information can be encoded. By arranging the QCA cells in some proper arrangements, it is possible to build logical elements and also transfer binarv information. QCA logic circuits is usually constructed with the binary wire, the inverter Gate and the three-input majority Gate [17, 18]. The QCA wire is a row of QCA cells, in which a binary signal propagates from left-to-right because of electrostatic interactions between adjacent cells. To make a complete logical set, we need an inverter Gate as shown in Figure

1b. The majority Gate can be built by five QCA cells as shown in Figure 1c, in which the cells a, b and c are the inputs and the cell f is the output with the following logic function [19, 20]:

$$f = ab + bc + ac = M(a, b, c) \tag{1}$$

Logic AND and OR functions can be implemented from the majority Gate by setting an input permanently to "0" or "1" values, respectively. The majority Gate is not a complete Gate in QCA technology. Using the inverter Gate and the three-input majority Gate every QCA logic circuit can be implemented.



Figure 1. The QCA (a): cell (b): inverter Gate (c): three-input majority Gate.

2. PROPOSED QCA DESIGNS

The objective of this paper is to propose and analyze different circuits for QCA sequential designs. In this paper, all of the proposed layouts are simulated using QCADesigner software [21] with the following parameters for a Bistable approximation: Cell size=18nm, Number of samples=20000, Radius of effect=90nm, Relative permittivity=12.9, Convergence tolerance=0.001, Clock high=9.8e-22J, Clock low=3.8e-23J, Clock amplitude factor =2, Layer separation=11.5nm and Maximum Iterations per sample =100. Also, each QCA cell is assumed to have the width and length of 18 nm, the neighbor cells have a center to center distance of 20 nm and quantum dots have 5 nm diameters.

2.1. D Flip-Flop

Flip-flops are the basic storage element in sequential logic. They are one of the main building blocks of digital circuits, which are used in the computer and communications, and many other types of systems. One of the most fundamental Flip-flops is the D flip-flop (DFF), which captures the value of input D at a definite portion of the clock cycle (Clock). At other times, the output Q does not change. The D flip-flop is widely used. It is also known as a "data" or "delay" flip-flop. The D flipflop can be viewed as a memory cell; a zero-order hold or a delay line. In Figure 2, the characteristic table and the symbol of D flip-flop are shown, where the inputs are D and C (Clock), the output is Q, and Q_0 means the previous state of Q. Using Figure 2, the output function of DFF and its equivalent expression based on the inverter and three-input majority Gates can be obtained by the following equation:

$$Q = C.D + C.Q_o =$$

 $M(M(C, D, -1), M(\overline{C}, Q_o, -1), +1)$ (2)

In Figure 3, one possible implementation of DFF and its simulation results for both $Q_0=-1$ and $Q_0=+1$ are shown.



Figure 2. DFF (*a*) *circuit symbol* (*b*) *characteristic table.*

OCADesigner software (Bistable approximation engine default with parameters) used to design is and simulation of the proposed DFF. The proposed DFF has the following specifications: the number of cells 46, the occupied area 0.0512 μm^2 and 4 phases input to output delay.



Figure 3. Proposed QCA DFF (a) layout (b) simulation results.

To solve the problem of physical level implementation of QCA clock signal, a more realistic clock distribution should be adopted. Figure 4 shows a logicpropagation technique for the 2-D diagonal wave scheme (2DDWave) [22].



Figure 4. Clocking for the 2-D wave propagation [22].

In this method, the QCA design must be partitioned into a perfect grid of zones such that all zones in a row have the same height and all zones in a column have the same width. Each zone must accept input signals only from two zones (north and west) and pass its outputs to the other two zones (south and east). Figure 5 shows the layout of proposed DFF with 2-D wave clocking and its simulation results.

To show the functionality of the proposed DFF in Figure 3, a 5-bit up counter is designed [13]. Figure 6 shows the layout and simulation results of proposed 5-bit counter. This counter is implemented with 368 QCA cells. It has an area of 0.81 um² and 6.5 clock cycles delay.

Recently, fault-tolerant properties of QCA circuits have been presented by several researchers [23, 14, 24]. The cell misplacement, cell misalignment, cell missing deposition and extra or additional cell defects are main defects in QCA implementations. In this section we present missing cell defects and identify the test vectors for detection of all faults for the proposed DFF.



Figure 5. Proposed DFF with 2-D wave clocking (a) Layout (b) simulation results.



Figure 6. Proposed 5-bit counter (a) Layout (b) simulation result.

Through all simulations, a particular cell labeled with the number i (i =1,2, ..., 42) (shown in Figure 7) is deleted in the original (defect-free) configuration of the proposed DFF and the new configuration is simulated using QCADesigner with Bistable engine.

The simulation results show that only deleting the cells with the numbers 3, 5, 7, 9, 14, 17, 20, 25 and 40 results faulty output in the output Q and deleting the other cells results no faulty output in the output Q. Also, for the input set {Clock D} = {00, 01, 10, 11} all distinct faulty outputs in the output Q are obtained: {0101, 1111, 0000, xxxx, 1100}, where x means Q has a polarization of "0" (Null). For detecting the effects of these defects, a test sequence can be utilized as: $\{Clock D\} = \{01, 11\}$ (for the defect-free output 0001 when $Q_0=0$ and {Clock D} = {00, 10, 11} (for the defect-free output 1101 when $Q_0=1$). These test vectors can detect any cell missing defects in the proposed DFF layout.



Figure 7. Layout of the proposed DFF for analysis of missing cell defects.

2.2. Single Edge Generator

Frequency dividers and (rising or falling) single edge generator (SEG) are some of DFF applications. By putting C=D in Equation (2), a rising SEG can be created. In this case, if the input is "In" and the output is "out" then:

$$out = In.In + \overline{In.out_o} =$$

$$In + \overline{In.out_o} = In + out_o$$
(3)

In Figure 8, the QCA implementation and simulation results of proposed SEG in QCADesigner are shown.



Figure 8. The proposed QCA SEG (a) layout (b) simulation results.

The proposed SEG has the following specifications: the number of cells 16, the occupied area 0.0161 μ m² and 3 phases input to output delay. In the proposed SEG, three phases after raising the input, the output rises and then remains in this state. This input to output delay can be changed by placing n-phase and m-phase wires in the input and output, respectively. In this case, in the proposed SEG, (3+m+n) phases after raising the input, the output rises and then remains in this state. Also, by placing an inverter Gate in the output, a falling SEG can be realized.

2.3. Divide-by-2 Counter

Another application of DFF is binary divider for frequency division or a divideby-2 counter. By putting $D = \overline{Q_o}$ in Equation (2), a divide-by-2 counter can be created. In this case, if the input is "In" and the output is "out", then:

 $out = In.\overline{out_o} + \overline{In.out_o} = In \oplus out_o$ (4)

In Figure 9, the QCA layout and simulation results of proposed divide-by-2 counter in QCADesigner are shown.

The proposed divide-by-2 counter has the following specifications: the number of cells 49, the occupied area 0.048 μ m² and 4 phases (1 clock cycle) input to output delay.



Figure 9. Proposed QCA divide-by-2 counter (a) layout (b) simulation results.

It can be seen from Figure 9b, that the output has a frequency that is exactly onehalf that of the frequency of input "In". In other words, the circuit produces frequency division as it now divides the input frequency by a factor of two. This can produce a type of counter called ripple counter, in which the clock pulse triggers the first flip-flop whose output triggers the second flip-flop and so on.

2.4. Oscillators

An electronic oscillator is an electronic circuit that produces a repetitive, oscillating electronic signal, often a sine wave or a square wave. Oscillators are widely used in many electronic devices. Oscillators are often characterized by the frequency of their output signals. The logical function for a selectable oscillator is given by:

$$Out = In.\overline{out_o} \tag{5}$$

where "In" is the activation input and "Out" is the output of selectable oscillator. By putting "In"=1 a permanent oscillator can be realized. Also, by using a SEG and a selectable oscillator, a positive-edgetriggered oscillator can be created, which is sensitive to the rising edge of its input. In Figure 10, the circuit diagram, QCA layout and simulation results of proposed oscillators are shown, where "Select OSC", "OSC" and "Edge OSC" are stand for the output of selectable, permanent and positive-edge-triggered oscillators, respectively. The proposed selectable and permanent oscillators have the following specifications: the number of cells 16, the occupied area 0.016 μ m² and 2 phases input to output delay. Also, the proposed positive-edge-triggered oscillator has the following specifications: the number of cells 38, the occupied area 0.049 μ m² and 7 phases input to output delay.

2.5. K-pulse Generator (KPG)

In Figure 11a, the circuit diagram of a positive-edge-triggered K-pulse generator is presented, where:

$$K = \frac{n+m}{4} \tag{6}$$

The proposed K-pulse generator is composed of two SEGs, one AND Gate, one inverter Gate, a wire with one phase delay (one-phase wire), an n-phase wire and an m-phase wire. In this circuit, the first output pulse is appeared six phases after the first rising edge of the input. In Figure 11b, the QCA layout of a positiveedge-triggered 4-pulse generator is shown. Also, Figure 11c shows the simulation results of proposed positive-edge-triggered K-pulse generator for K=1 (1-pulse generator), K=2 (2-pulse generator) and K=4 (4-pulse generator (Four PG)) in QCADesigner software, where Out1, Out2 and "Four PG" are stand for the outputs of proposed 1, 2 and 4-phase generators, respectively.

The proposed layout shown in Figure 11b has the following specifications: the number of cells 63, the occupied area $0.063 \ \mu\text{m}^2$ and 6 phases input to output delay.

2.6. Negative Pulse Generator (NPG)

The problem posed in this section is to devise a circuit with a single input P and a single output Q, which produces a short negative pulse whenever the input goes positive.



Figure 10. (a) Layout of proposed selectable oscillator (b) layout of proposed permanent oscillator (c) circuit diagram of proposed positive-edge-triggered oscillator (d) layout of proposed positive-edge-triggered oscillator (e) simulation results of proposed oscillators.



Figure 11. (a) Circuit diagram of proposed positive-edge-triggered K-pulse generator (b) layout of proposed 4-pulse generator (c) simulation results of proposed 1, 2 and 4-pulse generators.

This sort of circuit is encountered frequently, and many logic designers have met it and solved it one way or another usually by using a single-shot or some sort of logic delay line. Our circuit description only provides for a single stable output value. The negative pulse is generated on the rising edge of the input, and will automatically complete before stability returns. The equations for the circuit are: $\Omega - Y = \overline{P} + v_0$

$$Q = Y_1 = P + y_2$$
$$Y_2 = \overline{y_1} + Py_2$$

(7)

These equations are implemented in Figure 12.



Figure 12. Negative pulse generator (a) circuit diagram (b) proposed QCA layout (b) simulation results.

3. RESULTS AND DISCUSSIONS

The consumption power in the QCA arrays is 10⁻¹⁰W per input bit. In this research, DFF, single edge generator. positive-edge-triggered oscillator, negative pulse generator and edge-triggered K-pulse generator designs have 2, 1, 1, 1 and 1 inputs, respectively and thus the consumption powers of them are $2 \times 10^{-10} W$. $10^{-10}W$ $10^{-10}W$, $10^{-10}W$, and $10^{-10}W$. respectively. Fault-tolerant properties and characteristics of QCA for metal and molecular implementations have been reported by several researchers [25, 26]. The cell misalignment, cell misplacement, cell missing deposition, stuck-at-Z and extra or additional cell defects are the identified defects in QCA circuits. In this section, simulation of missing cell defects for the proposed NPG are presented. Through all simulations, a particular cell labeled with the number i (i = 1, 2, ..., 50)(shown in Figure 12) is deleted in the original (defect-free) configuration of the proposed NPG, and the new configuration is simulated using QCADesigner with its coherence vector engine with the following parameters: temperature 1 K, relaxation time 1 fs, time step 0.1 fs, total simulation time 70 ps, clock high $9.8 \times 10-22$ J, clock low $3.8 \times 10 - 23$ J, clock shift 0, clock amplitude factor 2, radius of effect 80 nm, relative permittivity 12.9, layer separation 11.5 nm, Euler method, and randomized simulation order. The simulation results show that deleting the cells with the numbers 1, and 3 results no faulty output in output "Q". Deleting the cells with the numbers 4-7 and 11, 12, 16 and 17 converts the proposed NPG to a positiveedge-triggered oscillator. Deleting the cells with the numbers 1-3, 8, 9, 14, 18-27, 38, 40, 42-46, and 48-50 results no faulty output in the output Q. Temperature has different effects on different QCA circuits. The robustness (producing high polarization correct response in different temperatures) of the proposed QCA designs is presented. This can be done with the measurement of output cells polarization (when the output is correct) in different temperature. Figure 13 shows the robustness results for the divide-by-two, Four PG and NPG designs. The simulation results show that all proposed QCA designs are able to produce correct results in the temperature range from 1K to 20K. As it can be seen, the performance of the proposed NPG is better than the other ones. It should be mentioned that the outputs of the proposed designs will not be broken down when temperature passes from 1K to 20K. Therefore, the proposed OCA designs are robust designs.

Figure 14 shows the layout of a 4 to 1 multiplexer implemented with 0.13µm CMOS technology. Table 1 shows the comparison between the proposed QCA design and the conventional CMOS technology. From Table 1, it is clear that the QCA design is more efficient in terms of area and clock frequency. For example, the proposed QCA negative pulse generator is more than 325 times smaller.

Table 2 shows a detailed comparison between the proposed DFF and the previous works in terms of occupied area, cell count and delay.



Figure 13. The robustness of proposed QCA designs.



Figure 14. Layout of negative pulse generator implemented with $0.13\mu m$ CMOS technology.

Table 1. Comparison with 0.13 µm CMOS technology.

NPG	Approximated area (µm ²)	Clock frequency (GHz)
Proposed QCA layout	0.052	28.5
0.13μm CMOS Technology	16.9	<3

From Table 2 it is clear that our presented QCA layout has a relatively good performance. From the obtained results, it can be seen that the proposed designs work satisfactory and produce correct outputs with highly polarized signals, which can provide a high drivability for QCA circuits.

 Table 2. Comparison with the previous

QCA works.				
References	Area (um ²)	Complexity (cell count)	Delay (clock cycle)	
Level triggered DFF [12]	0.05	48	1	
Falling edge triggered DFF [12]	0.09	84	2.75	
Rising edge triggered DFF [12]	0.09	84	2.75	
Dual edge triggered DFF [12]	0.14	120	3.25	
DFF-(I) [13]	0.1	74	1.5	
DFF-(II) [13]	0.02	28	0.5	
Proposed DFF	0.05	46	1.25	

4. CONCLUSIONS

Quantum-dot cellular automata (QCA) with its unique specifications reduces the physical limit of CMOS devices implementation. Thus it encourages researchers to utilize it in designing of integrated circuits. In this paper, new efficient designs for QCA DFF, single edge generator, oscillators, negative pulse generator and edge-triggered K-pulse generator were presented. The proposed designs were implemented and simulated using QCADesigner software without any wire crossing methods. Also. the robustness of proposed QCA designs was tested. The results showed that these designs work properly and can be simply used in designing of QCA sequential circuits.

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